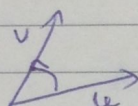


3 октябрь 2013 - Углубленная геометрия

u, v



$u \times v \rightarrow$ векторное произведение

$$\sin(u \times v, u \cdot v) = |u||v|(\sin(u, v), \cos(u, v))$$

a - число

s - скалярно

скалярно произв.

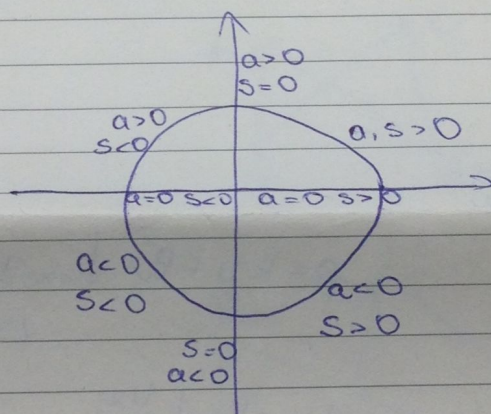
- т.е. угол

+ острый угол

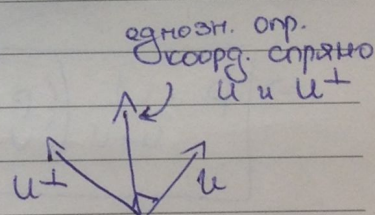
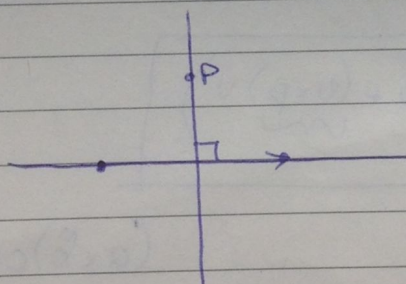
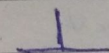
векторное произв.

если угол др.

предположение



black and white
ideas-notes-planes



$$k(u+v) = ku + kv$$

$$(k_1 + k_2)u = k_1u + k_2u$$

$$u(v_1 + v_2) = uv_1 + uv_2$$

$$u \times (v_1 + v_2) = u \times v_1 + u \times v_2$$

$$u \cdot v = v \cdot u$$

$$u \times v = -v \times u$$

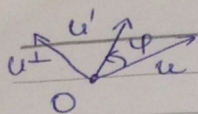
$$u \times v = u^{\perp} \cdot v$$

$$(u^{\perp})^{\perp} = -u$$

$$u^{\perp} \times v^{\perp} = u \times v$$

$$u^{\perp} \cdot v^{\perp} = u \cdot v$$

$$u \times v^{\perp} = u^{\perp} \cdot v^{\perp} = u \cdot v$$



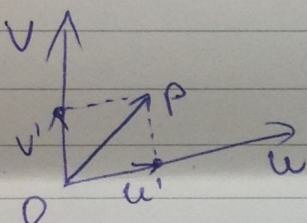
$$u' = \cos\phi \cdot u + \sin\phi \cdot u^\perp$$

$$(u \times v)^2 + (u \cdot v)^2 = u^2 \cdot v^2$$

$$\sin^2 \dots + \cos^2 \dots = 1$$

$$\frac{1}{2}(x_1 y_2 - x_2 y_1)$$

$$u \times v \neq 0$$



black and white
ideas notes plane

O_{uv}

$$p = ku + lv \mid \times v \rightarrow p \times v = k u \times v$$

$$\hookrightarrow k = \frac{p \times v}{u \times v}$$

$$p = ku + lv \mid \times u \rightarrow u \times p = l u \times v$$

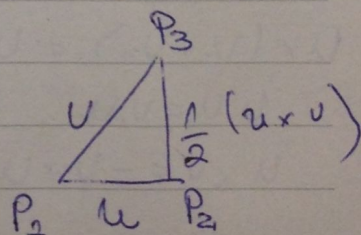
$$\hookrightarrow l = \frac{u \times p}{u \times v}$$

$$\Rightarrow \boxed{p = \frac{1}{u \times v} \left(\underbrace{(p \times v)}_k u + \underbrace{(u \times p)}_l v \right)}$$

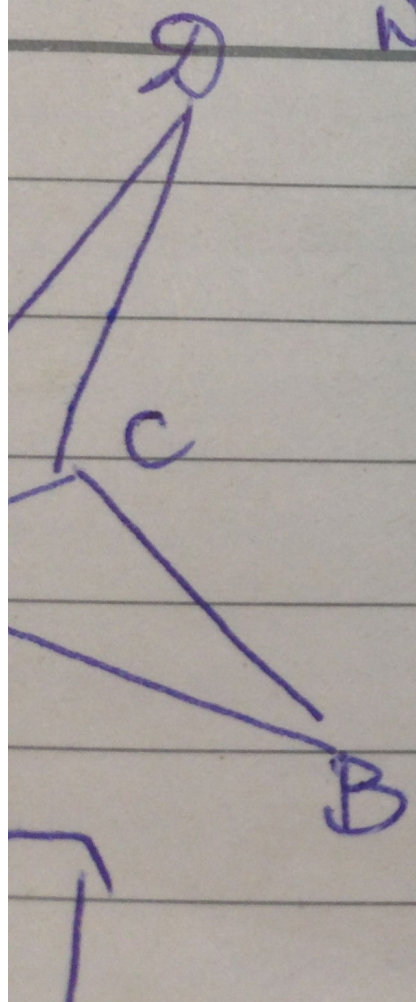
$$(a \times b)c + (b \times c)a + (c \times a)b = 0$$

$$u = \frac{u^\perp \cdot \frac{1}{u^2}}$$

$$u = u^\perp : p = \frac{1}{u^2} \left((u \cdot p) \cdot u + (u \times p) u^\perp \right)$$



$$= \frac{1}{2} (P_1 \times P_2 + P_2 \times P_3 + P_3 \times P_1) \quad -2-$$



nww. math. bas. ba / Bontchev
/ vecta (EUBH.)

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sketch, ps